

Kinetic Theory of Gases is?

Continued from Oct 9th

- **Isothermal Irreversible** ٠ **Expansion or Compression** in One Step:
- For expansion the external pressure must satisfy the expression
- $Pext \le p_2$, Let $Pext = p_2$ the work involved is
- $w = -Pext (\Delta V) =$ $p_2 (V_2 - V_1)$ (15) since $V_2 > V_1$. w = -ve fig 2
- displays the magnitude of work as the shaded area.
- For compression the external pressure must satisfy the expression $Pext \le p_1$, Let Pext =p1. The work involved is
- $w = Pext (\Delta V)$
- = $p_1 (V_1 V_2)$ (16) since $V_1 > V_2$. w = +ve, fig 3 displays the work as the sha ded area. Obviously |w_exp | <w_eump (17)
- If Pext \leq p2in expansion or Pext \leq p1 in compression the desired volume change may be carried out by using set of stops where the movement of piston gets arrested.



✤ Isothermal Irreversible **Expansion or Compression** in More than One Step:

- If the above mentioned expa -nsion or compression is carried out in more than one step, the Pext has to be adjusted in each step. Let pext be equal to the final pressure in each step.
- Figure 4 and 5 displays the magnitude of work involved in the expansion and the work involved in compre ssion carried out in two steps, respectively.





(19)

Note:

The magnitude of work

involved in reversible expan

sion is maximum is compa -

red to the involved in

The work involved in rever

sible compression is minim -

um as compared to that in

-volved in irreversible comp

For Adiabatic expansion or

compressure, heat is neither

enters nor leaves the system.

Hence dq=0. The first law of

 $w = -Pext(V_2 - V_1) - nCv(T_2)$

for expansion $V_2 > V_1$, w = <

0, hence $T_1 > T_2$. Thus cool ing

is observed during expansion.

For compression $V_2 \leq V_1, w =$

> 0, and hence $T_1 < T_2$. Thus

heating is observed during

Expansion or Compression:

The involved under rever -

sible conditions can be calcul

If the final temperature T2 is

not available, it can be

evaluated by the expressions

derived in the following. For

 $Pext = p \pm dp$ thus we have

the reversible conditions,

(21)

-ated from the expression

 $w = \Delta U - nC_{v1m}(T_2 - T_1)$

Adiabatic Reversible

or nCvdT=-Pext

thermodynamics gives

irreversible expansion.

* Adiabatic Irreversible

Expansion or

Compression:

-ression.

dU=dw

 $-T_1$) (20)

compression.

dVor

•

Notes:

- Comparing figs 2 and 4, we find that the magnitude of the work involved has increased in going from one-step to two-step expansion. This trend is continued as the number of steps is increased.
- Comparing figs 3 and 4, we find that the work involved has decreased in going from one-step to two-step compr ession. This trend is continu -ed as the number of steps is increased.
- ** **Isothermal Reversible Expansion or Compression:**
 - In reversible expansion or compression, the external pre -ssure differs infinitesimally from the pressure of gas. For expansion Pext = p - dpFor compression Pext = p + dpThe expression of work is $dw - Pext dV - (p \mp dp)dV =$ pdV (The product dpdV is

ignored as it involves infinite simal quantities)

For an ideal gas, p - nRT/V.

- $dw nRT\frac{av}{v}$ Hence (18)For a finite change, we have
- $w = -nRT \int_{v_1}^{v_f} \frac{dv}{v} = -nRT \ln \frac{v_f}{v_1} \quad (19)$
- For expansion $V_1(=V_2) >$ $V_1(=V_1)$, w is negative and the work is done by the system.
- For expansion $V_1(=V_1) >$ $V_1(=V_2)$, w is positive and work is done by on the system.
- Figure displays the magni tude of work involved in



 $T^{v}(\gamma^{-1}) = constant$ (23)In terms of pressure, we have

 $dU = dw \text{ or } nC_{v1m}dT = PextdV$ or $nC_{v1m}dT = (p\pm dp) dV = pdV$ Replacing p nRT/V; we get

or

or

or

or

or

(22

(25)

 $nC_{v1m}dT = -\left(\frac{nRT}{V}\right)dV$

for a finite change we have

 $C_{v1m}\frac{dT}{T} = -R\frac{dV}{V}$

 $T\left(\frac{RT}{T}\right)^{\gamma-1} = \text{constant}$ or $T^{\gamma}p^{1-\gamma} = \text{constant}$ (24)The relation between p and V is $\left(\frac{pV}{p}\right)V^{\gamma-1} = \text{constant}$ or

$pV^{\gamma} = \text{constant}$

- Equation (23) (25) hold good for an ideal gas undergoing adiabatic reversible expan sion or compression.
- * **Expansion Against Vacuum :** When the gas undergoes expansion (isothermal or adiabatic) against vacuum. pext = 0 Hence the work involved is dw = -Pext dV = 0 or w = 0
 - For such an expansion $\Delta V=0, \Delta H=0 \text{ and } \Delta q=0$ (26)

 Molecules 	Translational	Rotational	vibrational	Total	Cy1m	Cy1m	Y- Cv1m/Cv1m
Diatomic	$\frac{3}{2}$ RT	$2 \times \frac{1}{2}RT$	RT	$\frac{7}{2}$ RT	$\frac{7}{2}R$	$\frac{9}{7}R$	$\frac{9}{7}$ - 1.286
Triatomic Linear	$\frac{3}{2}$ RT	$2 \times \frac{1}{2}RT$	4RT	$\frac{13}{2}$ RT	$\frac{13}{2}R$	$\frac{15}{2}R$	$\frac{15}{2}$ - 1.153
nonlinear	$\frac{3}{2}$ RT	$2 \times \frac{1}{2}RT$	3RT	6RT	6RT	7RT	$\frac{7}{6} - 1.167$

Heat Capacities of Gases: The absorption of heat by gases causes an increase in (i) kinetic (or translation) ene rgy, (ii) rotational energy, and



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Hence, $C_v = \left(\frac{\partial E_k}{\partial T}\right)_v = \frac{3}{2} nR$ and $C_{v1m} = \frac{3}{2}R$ (27) Monoatomic gaseous molecules have only translational motion and thus $C_{\nu 1m} = \frac{3}{2}$ R; $C_{\nu 1m} = \frac{3}{2}$ R + R = $\frac{5}{2}$ R; $\gamma = \frac{c_{pm}}{c_{vm}} = \frac{5}{3} = 1.667$ (28)

(iii) vibration energy of gaseous molecules.

- The kinetic energy as given by kinetic theory of gases is Ek = 3/2 nRT
- Diatomic and polyatomic gaseous molecules. Besides having translation motions, also have rotational and vibrational motions.
- Linear and nonlinear molecules have two and three independent rotational mot ions respectively, and each contribute (1/2) NT towards molar energy of the molecule.
- Linear and nonlinear • molecules have 3N 5 and 3N 6 independent vibrational motions, respectively, where N is the number of atoms in the molecule. Each vibrat ional motion contributes RT towards molar energy of the molecule.
- The following is the summ ary of molar energy contri -butes by each motion towards the total molar energy of the molecules. It also includes, their heat capacities and the ratio of heat capacities.
- **Comment :** The contribution of vibrational motion towards

	JAI	ONT	/ 11	$\frac{-1.167}{6}$	
heat	cap	acity	is effe	ective onl	ly
at hi	ghe	r tem	oeratu	res (whic	h
depe	end	s on th	ne nati	ure of gas	s)
and	thu	s at o	rdinar	y temper	ra
-tur	e th	nere i	s con	tribution	ıs
fron	n tra	anslati	ion an	d rotatio	-
nal 1	not	ions.	This g	ives lowe	er
valu	les (of C	Vw.		

